

## Statistics 7220 Predictive Analytics

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### Overview

This half-semester course introduces predictive techniques that extend beyond regression analysis introduced in courses such as Stat 102 or Stat 621. These extensions select the most predictive model, classify observations into categories, and partition data into homogeneous subsets. The emphasis is conceptual, focused on the motivation for and properties of various methodologies.

Illustrative applications use real data, typically with more cases and variables than encountered in intro courses. The datasets are “tabular”, with features organized into columns and cases into rows as if the cases have been sampled independently from some population. To focus our analysis, these datasets are “clean” – without missing data or common coding errors. Other courses cover unstructured data (text, images) and sequential data (time series). These are not covered here.

This course divides into four segments. The first two segments emphasize statistical inference using tests and p-values to judge the predictive ability of models. The first segment reviews least squares, emphasizing interpretation, nonlinear and categorical features, and diagnostics. The second segment introduces logistic regression for classification, as in predicting the choice made by a consumer. Examples use held-back data to illustrate how statistical tests anticipate results when fitted models are applied to new data.

The last two segments adopt the spirit of machine learning, relying on held-back data in place of statistical tests. The third segment covers model selection. Models often look better when built than realized in practice, particularly when the modeler chooses from among many potentially predictive features. Statistics avoids such over-confidence by employing a theoretical “model selection criterion” whereas machine learning requires held-back data. Key among these is the lasso. The fit from a lasso is nonetheless familiar, an equation with estimated coefficients.

The final segment introduces models that avoid the explicit, equation-based structure of regression. Tree-based models partition the sample, collecting observations into batches whose average responses serve as predictions. Versions of this approach that combine many trees have a strong reputation in practice and rival neural networks when building predictive models from tabular data.

## Prerequisites

With only half a semester to cover these topics, this course moves at a brisk pace and presumes students are familiar with inferential statistics, such as the use and interpretation of hypothesis tests, confidence intervals, and  $p$ -values. Students should also be familiar with applied multiple regression analysis, specifically least squares regression (including  $R^2$ , RMSE, various  $t$ - and  $F$ -tests, confidence/prediction intervals, and residual diagnostics). Prior exposure to logistic regression and Bayesian statistics is helpful but not required.

The course presumes some familiarity with the statistics package JMP. This is not a programming course and instead relies on the built-in capabilities of this point-and-click software to illustrate the practical use of the covered methods. Students are encouraged to use on-line resources, particularly ChatGPT, for guidance on how to run this software.

## Materials

Class notes provide background for the methods and examples covered in lectures; these will be distributed via Canvas. These notes cover some details but rely on the required textbook for further explanation:

*An Introduction to Statistical Learning, 2<sup>nd</sup> Edition* (2021, abbreviated ISL)  
James, Witten, Hastie, and Tibshirani

[https://hastie.su.domains/ISLR2/ISLRv2\\_website.pdf](https://hastie.su.domains/ISLR2/ISLRv2_website.pdf)

Datasets and supplemental materials are located at

<https://www.statlearning.com/resources-second-edition>

This text uses the R statistical modeling environment (another edition uses Python); as noted, we'll use JMP to avoid the overhead of learning how to program while also learning the methodology. JMP is available via Canvas.

Further background reading that covers multiple regression may be found in the following casebook and text (used in some Wharton classes).

*Business Analysis Using Regression*. Foster, Stine, and Waterman; Springer, 1998.

*Business Statistics* (BS) Stine and Foster, Addison-Wesley, 2010.

## Office hours and TA

A schedule for TA hours will be posted in Canvas.

My office hours are on Monday and Wednesday afternoons from 3:30 to 5:30 p.m. Otherwise the best way to contact me is by e-mail.

## Requirements

Total grade = 75% assignments + 25% final cumulative test

All relevant University policies regarding Academic Integrity must be followed in regard to assignments and tests.

### *Attendance*

Students are expected to attend class. Video access will be made available upon request to students who do not attend class only when accompanied by formal absence documentation (usually via an academic advisor).

### *Assignments*

Weekly data analyses problem sets reinforce classroom discussion and develop hands-on familiarity with the use of course methods.

- Assignments are weekly and solutions are reviewed on the day assignments are turned in. Hence, assignments must be turned in on-time to receive credit. Don't wait until the last minute to complete the work.
- Each student must submit solutions to an assignment expressed in his or her own words. It is okay to discuss assignments with classmates, but the assignments are to be written up independently.
- Assignments must be turned in during class by the submitting student.
- All questions about the grading of an assignment must be resolved within one week of the date on which the graded assignment is returned.

### *Cumulative Test*

The final test will be closed book (one page of notes), during the final class period. For this quarter, the final test will be on February 28.

### *ChatGPT*

Within this class, you are welcome to use AI tools in an unrestricted fashion at no penalty. You should be aware that tools based on large language models such as GPT may make up incorrect facts and fake citations. You will be responsible for inaccurate, biased, offensive, or otherwise unethical content you submit regardless of whether it comes from you or an AI assistant. Having said this, the use of an AI program is encouraged, as it may make it possible for you to submit assignments with higher quality, in less time. The university's policy on plagiarism still applies to any uncited or improperly cited use of work by other human beings, or submission of work by other human beings as your own.

## Overview of Course Topics

We won't spend a day on each module; some later in the course take more time. Consider sections of these notes not covered in class to be supplemental, as if from portions of the course textbook that you skim rather than read carefully.

*Be aware:* I will occasionally revise these notes that are posted on-line to correct errors or omissions and to elaborate topics that arise in class discussion. Check the revision date found at the bottom of the first page of each module.

### *Multiple Regression*

*ISL, Ch 1-3*

#### *Module 1.0 Review example*

The methods illustrated in this regression analysis should be familiar. We will not explicitly cover this model in class, but you will need to know this material in later modules.

#### *Module 1.1 Multiple regression*

Further details of multiple regression, emphasizing interpretation, inference, and diagnostics.

#### *Module 1.2 Categorical explanatory variables*

Regression models make heavy use of group information in the form of categorical variables and their interactions with other features. Questions of multiplicity arise.

#### *Module 1.3 Calibration*

Every predictive model should be calibrated. It is easy to check, "low-hanging fruit". There's no reason not to.

### *Readings*

Skim chapters 1-2 of ISL. We'll not use R, so skip those portions such as Sections 2.3 and 3.6 unless you're interested. We will not cover K-means clustering, but it's easy to understand for the sake of reading the comparisons offered in Section 3.5. BTW, JMP makes it easy to construct 3-D figures like Figure 3.4 or 3.5.

### *Classification*

*ISL, Ch 4*

#### *Module 2.1 Simple logistic regression*

When the response that you want to predict is categorical, you're in the domain of generalized regression. We start with models having one predictor to figure out how to fit and interpret logistic regression. No more least squares.

#### *Module 2.2 Multiple logistic regression*

Logistic regression can use more than one predictor, just like least-squares regression. Once we allow several predictors, how are we supposed to decide which features belong in a multiple logistic regression? Once we identify them, what do they mean?

### **Readings**

Focus on Section 4.3 that introduces logistic regression. ISL includes an alternative classifier known as linear discriminant analysis (LDA) which is basically least squares regression fit to a dummy variable. Skim the details of LDA and focus on the use of logistic regression. Notice that important methods for evaluating a classifier (*e.g.* ROC curve, confusion matrix) are introduced in the discussion of LDA (pages 150-152). If you go further into “machine learning”, you’re likely to run into naïve Bayes (Section 4.4.4) so don’t skip this part. Skim (or omit if you’re pressed for time) the discussion of QDA and Poisson regression in Section 4.6. The discussion of QDA alerts you to assumptions of LDA; Poisson regression illustrates a type of regression designed for counts.

### **Model Selection**

#### **Module 3.1 Over-fitting**

*ISL, Ch 6, Sec 7.1*

It’s easy to pick the model if you only have a few predictive features, but what if you have thousands? Once you recognize the importance of interactions, the set of possible models grows geometrically. Greedily picking the best apparent choice using an procedure such as stepwise regression typically leads to over-fitting: the fitted model looks better than when applied to new data.

#### **Module 3.2 Cross validation**

*ISL, Ch 5*

Regression models often claim to do better than they actually can. The problem is most apparent when we test a model using the same data that we used to pick the model. Cross-validation avoids this problem by setting aside data for testing the model. Variations on this theme include repeating the process and recognizing that cross-validation itself makes an optimistic assessment of the model.

#### **Module 3.3 Model selection techniques**

*ISL, Sec 6-6.2*

Cross-validation helps, but becomes slow (and inconsistent) when applied more generally. Instead, penalty methods (ridge and lasso) and selection criteria (AIC, BIC) filter down the collection of competitive models with less computation. For example, the Bonferroni method limits the model to predictors that provide assured gains in accuracy.

### **Readings**

Concerns about model selection run throughout the text, starting from Chapter 2 onward (*e.g.* peek back at Section 2.2). We won’t spend time with bootstrap resampling (Section 5.2), so skim this discussion so you can appreciate the analysis in Section 5.3. We

won't cover PCA or partial least squares (Section 6.3), but you may run into these in other courses.

### ***Partitioning***

*ISL, Sec 2.2, Ch 8*

#### ***Module 4.1 Trees***

In a general sense, all statistical models work by averaging. The question is which observations to average. Regression models use an equation to identify which observations should be used to predict new data. Alternatives based on partitioning the data are more direct. Just look and see which observations are close to each other. Decision trees do this partitioning recursively.

#### ***Module 4.2. Forests and boosted trees***

Trees are natural, but often unstable (illustrating the bias/variance trade-off introduced in Chapter 2). We gain stability (at the cost of interpretation) by averaging over many trees. Boosting combines lots and lots of little trees (*a.k.a.*, shrubs, perhaps taking the analogy too far). A specific implementation of this approach (XGBoost) has become a reference method in many fields of application.

#### ***Readings***

JMP simplifies the construction of decision trees, so you can incrementally see (and control) how the method partitions the sample. We won't cover Bayesian additive regression trees (Sec 8.2.4), so skim that material.